

## Finding the Least Common Multiple (Denominator)

There are several ways that we can find the LCM of two or more numbers.

- 1) List out multiples of both numbers until we find a pair that match. This can become **long** and **tedious** if the numbers are large enough.

The LCM of 12 and 15 is 60 because

12: 12, 24, 36, 48, 60, 72, 84, 96, 108, 120, ...

15: 15, 30, 45, 60, 75, 90, 105, 120, ...

- 2) Ladder method: Divide out the numbers as a set, starting with "2" and going through every **prime** number.
  - A. Divide "2" from every possible number we're examining. If "2" doesn't go into a number, we just bring that number down. Continue doing this with the left over numbers until "2" can't go into anything.
  - B. Divide "3" from every possible number. If "3" doesn't go into a number, we just bring that number down. Continue doing this with the left over numbers until "3" can't go into anything.
  - C. Continue this process with all prime numbers until everything has divided out to "1"s.

The LCM of 12 and 15 is 60 because

$$2 \begin{array}{|l} 12 \\ 15 \end{array} \downarrow$$

$$2 \begin{array}{|l} 6 \\ 15 \end{array} \downarrow$$

$$3 \begin{array}{|l} 3 \\ 15 \end{array}$$

$$5 \begin{array}{|l} 1 \\ 5 \end{array}$$

$\swarrow$   $\begin{array}{|l} 1 \\ 1 \end{array}$  ← All "1"s means we're done!

$$\text{LCM} = 2 \cdot 2 \cdot 3 \cdot 5 = 60$$